# **GRAPHICAL FEATURES AND TERMINOLOGY COMMON CORE ALGEBRA I**

There is a lot of terminology associated with the graph of a function. Many of the terms have names that are descriptive, but still, work is needed to master the ideas.

*Exercise* #1: The function y = f(x) is shown graphed below over the interval  $-7 \le x \le 7$ .

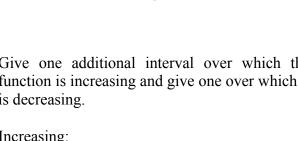
- (a) Find the maximum and minimum values of the function. State the values of *x* where they occur as well.
- (b) What is the y-intercept of the function? Explain why a function cannot have more than one y-intercept.
- (c) Give the x-intercepts of the function. These are also known as the function's zeroes because they are where f(x) = 0.
- (d) Would you characterize the function as increasing or decreasing on the domain interval  $-5 \le x \le -1$ ? Explain your choice.
- (e) Give one additional interval over which the function is increasing and give one over which it is decreasing.

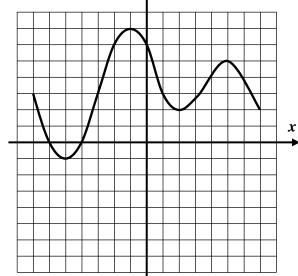
Increasing:

Decreasing:

- (f) The following points are known as turning points. Each can be classified as a relative maximum or a relative minimum. State which you think each is.
  - (-5, -1)(-1,7)(2,2)(5,5)relative minimum relative minimum relative minimum relative minimum or or or or relative maximum relative maximum relative maximum

COMMON CORE ALGEBRA I, UNIT #3 - FUNCTIONS - LESSON #4 eMATHINSTRUCTION, RED HOOK, NY 12571, © 2013





Date:



relative maximum



Let's get some more practice with **piecewise defined functions** and mix in our **function terminology** while we are at it.

*Exercise* #2: Consider the piecewise linear function given the equation  $f(x) = \begin{cases} x+3 & x \le 1 \\ 6-2x & x \ge 1 \end{cases}$ .

(a) Create a table of values for this function below over the interval  $-4 \le x \le 4$ . Then create a graph on the axes for this function.

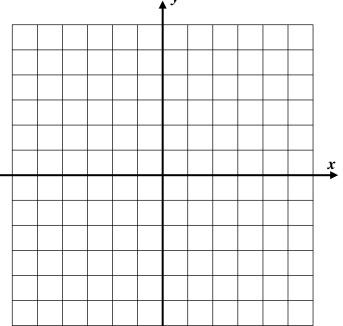
x	Rule/Calculation	(x, y)
-4		
-3		
-2		
-1		
0		
1		
2		
3		
4		

- (b) State the **zeroes of the function**.
- (d) Give the interval over which the function is increasing. Give the interval over which it is decreasing.

Increasing:

Decreasing:

(f) Use your graph to find all solutions to the equation f(x) = 2. Illustrate your solution graphically and find evidence in the table you created.



- (c) State the function's *y*-intercept.
- (e) Give the coordinates of the one turning point and classify it as either a relative maximum or relative minimum.
- (g) State the interval over which this function is positive. How can you tell this quickly from the graph?





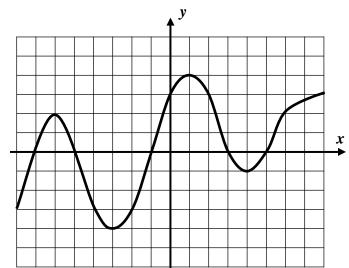
## GRAPHICAL FEATURES Common Core Algebra I Homework

#### FLUENCY

- 1. The function y = f(x) is shown graphed below over the interval  $-8 \le x \le 8$ .
  - (a) Evaluate each of the following;

$f\left(-2\right) =$	f(8) =
f(-8) =	f(4) =

(b) Find all the relative maximum and minimum values of the function. State the values of *x* where they occur as well.



- (c) What are the absolute maximum and absolute minimum values of the function? At what *x*-values do they occur?
- (d) What are the x and y-intercept(s) of the function? List each of the following as an ordered pair (x, y).

y-intercept(s):

(e) Give an interval over which the function is increasing. Give an interval over which it is decreasing.

Increasing:

Decreasing:

(f) Use your graph to find all solutions to the equation f(x) = 3. Illustrate your solution graphically.

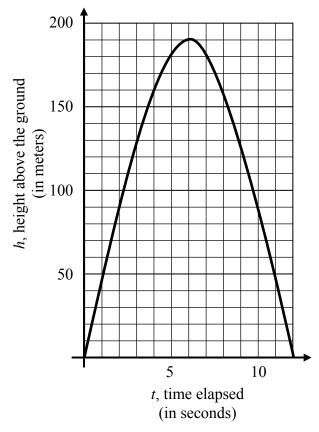
(g) Is the function positive or negative on the interval -1 < x < 3? How can you quickly tell?





#### APPLICATIONS

- 2. The following graph shows the height, h, above the ground of a toy rocket t seconds after it was fired. Use the graph of h(t) to answer the following questions.
  - (a) What was the maximum height the rocket reached? After how many seconds?
  - (b) How many seconds was the rocket in flight?
  - (c) Interpret h(2) = 90.
  - (d) Give the interval for *t* over which the height of the rocket is decreasing.



### REASONING

3. On the following set of axes, create the graph of a function f(x) with the following characteristics:

Passes through the points,

(-8,0), (5,-2) and (8,3)

Has an absolute maximum at f(-4) = 5

Has an absolute minimum at f(2) = -6

Decreasing on the interval on the interval  $-4 \le x \le 2$ 

