$\qquad$ Date: $\qquad$

## Introduction to Functions Common Core Algebra II



Most higher level mathematics is built upon the concept of a function. Like most of the important concepts in mathematics, the definition of a function is simple to the point of being easily overlooked. Make sure to know the following definition:

DEFINITION: A function is any "rule" that assigns exactly one output value ( $y$-value) for each input value ( $x$-value). These rules can be expressed in different ways, the most common being equations, graphs, and tables of values. We call the input variable independent and output variable dependent.

Exercise \#1: An internet music service offers a plan whereby users pay a flat monthly fee of $\$ 5$ and can then download songs for 10 cents each.
(a) What are the independent and dependent variables in this scenario?

Independent:
Dependent:
(b) Fill in the table below for a variety of independent values:

| Number of downloads, $x$ | 0 | 5 | 10 | 20 |
| :---: | :---: | :---: | :---: | :---: |
| Amount Charged, $y$ |  |  |  |  |

(c) Let the number of downloads be represented by the variable $x$ and the amount charged in dollars be represented by the variable $y$. Write an equation that models $y$ as a function of $x$.
(d) Based on the equation you found in part (c), produce a graph of this function for all values of $x$ on the interval $0 \leq x \leq 40$. Use a calculator TABLE to generate additional coordinate pairs to the ones you found in part (b).


Exercise \#2: One of the following graphs shows a relationship where $y$ is a function of $x$ and one does not.
(a) Draw the vertical line whose equation is $x=3$ on both graphs.
(b) Give all output values for each graph at an input of 3 .

Relationship A:
Relationship B:
(c) Explain which of these relationships is a function and why.



Exercise \#3: The graph of the function $y=x^{2}-4 x+1$ is shown below.
(a) State this function's $y$-intercept.
(b) Between what two consecutive integers does the larger $x$ intercept lie?
(c) Draw the horizontal line $y=-2$ on this graph.
(d) Using these two graphs, find all values of $x$ that solve the equation below:

$$
x^{2}-4 x+1=-2
$$


(e) Verify that these values of $x$ are solutions by using STORE on your graphing calculator.
$\qquad$

## Introduction to Functions Common Core Algebra II Homework

## Fluency

1. Determine for each of the following graphed relationships whether $y$ is a function of $x$ by using the Vertical Line Test.
(a)

(b)



(e)


2. What are the outputs for an input of $x=5$ given functions defined by the following formulas:
(a) $y=3 x-4$
(b) $y=50-2 x^{2}$
(c) $y=2^{x}$

## Applications

3. Evin is walking home from the museum. She starts 38 blocks from home and walks 2 blocks each minute. Evin's distance from home is a function of the number of minutes she has been walking.
(a) Which variable is independent and which variable is dependent in this scenario?
(b) Fill in the table below for a variety of time values.

| Time, $t$, in minutes | 0 | 1 | 5 | 10 |
| :---: | :--- | :--- | :--- | :--- |
| Distance from home, $D$, in blocks |  |  |  |  |

(c) Determine an equation relating the distance, $D$, that Evin is from home as a function of the number of minutes, $t$, that she has been walking.
(d) Determine the number of minutes, $t$, that it takes for Evin to reach home.

## REASONING

4. In one of the following tables, the variable $y$ is a function of the variable $x$. Explain which relationship is a function and why the other is not.

| $x$ | $y$ |
| :---: | :---: |
| -2 | 11 |
| 0 | 7 |
| 2 | 11 |
| 4 | 23 |
| 6 | 43 |
| $x$ | $y$ |
| 0 | 0 |
| 1 | -1 |
| 1 | 1 |
| 4 | -2 |
| 4 | 2 |

Relationship \#1 Relationship \#2

